

# Water Chemistry

# Water Chemistry

# The Chemical Processes and Composition of Natural and Engineered Aquatic Systems

Second Edition

Patrick L. Brezonik and William A. Arnold





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Published in the United States of America by Oxford University Press 198 Madison Avenue, New York, NY 10016, United States of America.

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Library of Congress Control Number: 2022938288 ISBN 978-0-19-765189-6 (pbk.) ISBN 978-0-19-760470-0 (hbk.)

DOI: 10.1093/oso/9780197604700.001.0001

1 3 5 7 9 8 6 4 2

Paperback printed by Lakeside Book Company, United States of America Hardback printed by Bridgeport National Bindery, Inc., United States of America

### Once again, to our extended families:

Carol Brezonik Craig and Laura Nicholas and Lisa and Sarah, Joe, Billy, Niko, and Peter

> Thomas and Carol Arnold Lora Arnold and Alex and Ben

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## Preface to the Second Edition

Over the past decade, we often wondered why, after taking on the arduous task of writing a textbook, would someone want to write a second edition? After over 10 years of using the book and getting feedback from colleagues and ideas from students, we realized, however, that the book's content and structure needed to be refreshed. In some cases, we were getting frustrated with our previous decisions on topic coverage and order of presentation. The topics covered in this edition are largely the same as the first edition, but in some cases the presentation has been altered. In other cases, updated information has been added to encompass the large quantity of new knowledge in the literature of the past decade. More advanced materials were moved and additional topics were added as web-based content so as to not add too much length to the physical (or electronic) book. We also changed the software used for chemical equilibrium calculations to VMINTEQ, which is freeware, and the kinetics software to Tenua, which is open source. We hope this will make the software-text linkage available to a broader audience.

As in the first edition, Part I (Chapters 1 and 2) provides an overall introduction to the field of water chemistry. Part II provides information about the underlying concepts necessary to understand the chemistry of aquatic systems: thermodynamics (Chapter 3), activity (Chapter 4), kinetics (Chapter 5), and basic organic chemistry (Chapter 6). The primer on organic chemistry was included here because many acids/bases and ligands mentioned in Part III are organic chemicals.

Problem-solving is emphasized in Part III: Chemical equilibria and kinetics. Chapters 7 and 8 were substantially revised and reorganized, with Chapter 7 discussing the fundamentals of acids and bases and the equations needed to solve problems. Chapter 8 presents the techniques (algebraic, graphical, and computational) to solve the systems of equations that define acid-base equilibria and uses the carbonate system to bring all the pieces together. The effects of global climate change and increasing atmospheric carbon dioxide levels on the inorganic chemistry of natural waters are given increased focus. These chapters are followed by complexation (Chapter 9), solubility (Chapter 10), and redox (Chapter 11). Two more chapters now are included in this section: surface chemistry (including that of nanoparticles) and sorption (Chapter 12) and the chemistry of organic pollutants (Chapter 13). Our thought here is that the concepts flow from the previous chapters and that instructors will likely want to introduce students to these topics in a single semester class.

Part IV has similar topics, although in a different order, as the first edition. Instructors can pick and choose the chapters to be covered depending on the focus of their class. Photochemistry (Chapter 14) builds on concepts of kinetics, and concepts of acid/base equilibria, redox, and kinetics are important in chlorine and

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oxidant chemistry (Chapter 15). We see these chapters (or parts of them) as likely to be included in engineering-oriented classes. Chapters 16–20 provide perspectives on water chemistry in natural systems. We provide more depth on mineral weathering and the biogeochemistry of iron, manganese, and aluminum than in the first edition. We also describe the kinds of chemical inferences facilitated by stable isotope fractionation techniques and by advances in computer technology that enable analysis of large datasets encompassing broad spatial or temporal scales. The chapter on natural organic matter was completely reorganized and updated. Indeed, all the chapters in Part IV were revised to include insights gleaned from the past decade of research.

Many examples in the chapters have been updated, and additional end-of-chapter problems were created. Users of the second edition will find the substantially revised and expanded companion website to be more useful than the previous version. In addition to web boxes of supplemental information on many topics, the site has complete reference citations for each chapter; abbreviated versions of references are given in the book to save space. Spreadsheets of datasets needed to solve many end-of-chapter problems also are on the website so that students do not need to retype the data in solving problems.

We hope these changes will benefit both students and instructors. We appreciate everyone around the world who has used the book as an instructor, student, practitioner, and researcher. Your feedback has been most helpful, and we sincerely hope you find the second edition even more useful than the first one.

Finally, although this book is heavily oriented toward problem-solving, we think it also is useful to keep in mind the following:

Rather than a problem to be solved, the world is a joyful mystery to be contemplated with gladness and praise.\*

—Patrick L. Brezonik and William A. Arnold University of Minnesota April 2022

<sup>\*</sup> Francis I, Laudato Si'. On Care for our Common Home. Vatican, Rome, 2015.

## Preface to the First Edition

In deciding whether to write a new textbook in any field, authors must answer two questions: (1) is there a need for another text in the field, and (2) how will their text be different from what is already available? It is obvious from the fact that this book exists that we answered yes to the first question. Our reasons for doing so are based on our answers to the second question, and they are related to the broad goals we set for coverage of topics in this book. Although previous introductory water chemistry textbooks provide excellent coverage on inorganic equilibrium chemistry, they do not provide much coverage on other topics that have become important aspects of the field as it has developed over the past few decades. These include non-equilibrium aspects (chemical kinetics) and organic chemistry—the behavior of organic contaminants and the characteristics and behavior of natural organic matter. In addition, most water chemistry textbooks for environmental engineering students focus their examples on engineered systems and either ignore natural waters, including nutrient chemistry and geochemical controls on chemical composition, or treat natural waters only briefly. This is in spite of the fact that environmental engineering practice and research focuses at least as much on natural systems (e.g., lakes, rivers, estuaries, and oceans) as on engineered systems (e.g., water and wastewater treatment systems and hazardous waste processing). Most existing textbooks also focus on solving inorganic ionic equilibria using graphical and manual algebraic approaches, and with a few exceptions, they do not focus on the use of computer programs to solve problems.

This book was written in an effort to address these shortcomings. Our overall goals in this textbook are to provide readers with (1) a fundamental understanding of the chemical and related processes that affect the chemistry of our water resources and (2) the ability to solve quantitative problems regarding the behavior of chemical substances in water. In our opinion, this requires knowledge of both inorganic and organic chemistry and the perspectives and tools of both chemical equilibria and kinetics. The book thus takes a broader approach to the subject than previous introductory water chemistry texts. It emphasizes the use of computer approaches to solve both equilibrium and kinetics problems. Algebraic and graphical techniques are developed sufficiently to enable students to understand the basis for equilibrium solutions, but the text emphasizes the use of computer programs to solve the typically complicated problems that water chemists must address.

An introductory chapter covers such fundamental topics as the structure of water itself, concentration units and conversion of units, and basic aspects of chemical reactions. Chapter 2 describes the chemical composition of natural waters and includes discussions on the basic chemistry and water quality significance of major and minor inorganic solutes in water, as well as natural and human sources and geochemical controls on inorganic ions. Chapters 3-7 cover important fundamentals and tools needed to solve chemical problems. The principles of thermodynamics as the foundation for chemical equilibria are covered first (Chapter 3), followed by a separate chapter on activity-concentration relationships, and a chapter on the principles of chemical kinetics. Chapter 6 provides basic information on the structure, nomenclature, and chemical behavior of organic compounds. Engineers taking their first class in water chemistry may not have had a college-level course in organic chemistry. For those who have had such a course, the chapter serves as a review focused on the parts of organic chemistry relevant to environmental water chemistry. Chapter 7 develops the basic tools—graphical techniques, algebraic methods, and computer approaches—needed to solve and display equilibria for the four main types of inorganic reactions (acid-base, solubility, complexation, and redox). The equilibrium chemistry and kinetics of these major types of inorganic reactions are presented as integrated subjects in Chapters 8-11.

Of the remaining eight chapters, six apply the principles and tools covered in the first 11 chapters to specific chemicals or groups of chemicals important in water chemistry: oxygen (12), disinfectants and oxidants (13), minor metals, silica, and silicates (15), nutrients (16), natural organic matter (18), and organic contaminants (19). The other two chapters describe two important physical-chemical processes that affect and sometimes control the behavior or inorganic and organic substances in aquatic systems: Chapter 14 describes how solutes interact with surfaces of solid particles (sorption and desorption), and Chapter 17 describes the principles of photochemistry and the role of photochemical processes in the behavior of substances in water.

The book includes more material and perhaps more topics than instructors usually cover in a single-semester course. Consequently, instructors have the opportunity to select and focus on topics of greatest interest or relevance to their course; we recognize that the "flavor" and emphasis of water chemistry courses varies depending on the program and instructor. Those wishing to emphasize natural water chemistry, for example, may wish to focus on Chapters 12, 15, 16, and 18 after covering the essential material in Chapters 1–11; others who want to focus on engineered systems and contaminant chemistry may want to focus more on Chapters 13, 14, and 19. Within several chapters, there also are *Advanced Topic* sections that an instructor may or may not use. With supplementary material from the recent literature, the book also may be suitable for a two-quarter or two-semester sequence.

A strong effort was made to write the text in a clear, didactic style without compromising technical rigor and to format the material to make the book inviting and accessible to students. We assume a fairly minimal prior knowledge of chemistry (one year of general chemistry at the college level) and provide clear definitions of technical terms. Numerous in-chapter examples are included to show the application of

theory and equations and demonstrate how problems are solved, and we have made an effort to provide examples that are relevant to both natural waters and engineered systems. The problems included at the end of most of the chapters generally are ordered in terms of difficulty, with the easiest problems coming first.

—Patrick L. Brezonik and William A. Arnold University of Minnesota February 2010

# Acknowledgments for the Second Edition

When we started down the path of a second edition, we reached out to many colleagues for their suggestions. We thank those who enthusiastically responded with ideas, input, and frustrations; we tried our best to incorporate your feedback. Once again, we greatly benefited from the knowledge of those willing to review chapters (in parentheses) when a fresh perspective was needed. We thank Paul Capel (1, 2), Erin Surdo (7, 8, 13), Teng Zeng (7, 8, 13), Chanlan Chun (9, 10), Brandy Toner (12), Kris McNeill (14), Mike Dodd (15), Bruce Monson (16), Mark Brigham (16), and Paul Bloom (20). Special thanks to Yu-Ping (Yo) Chin for doing double duty (Chapters 11 and 20) and providing many valuable insights and references.

To the hundreds of students at the University of Minnesota who noted errors, confusing explanations, and typos in the first edition, we appreciate your keen eyes. We especially thank our spouses for their patience and understanding during this two-year effort. Special thanks to Nick Brezonik for his contribution of the book cover photos for this and the first edition, Alex Arnold for his help editing the numerous equations, and Grant Goedjen for generating Figure 8.5. Last, we gratefully acknowledge our recently passed friend and colleague, Deborah Swackhamer, for her enthusiastic and dedicated efforts to ensure that water pollution was understood and taken seriously from a fundamental, scientific perspective.

# **Acknowledgments for the First Edition**

We owe a great debt of gratitude to the individuals whose reviews of individual chapters provided many comments and suggestions that improved the content of the book, and we appreciate their efforts in finding errors. We list them here alphabetically with chapters reviewed in parentheses: Larry Baker (1, 2, 16), Paul Bloom (18), Steve Cabaniss (18), Paul Capel (4, 6, 19), Yu-Ping Chin (18, 19), Joe Delfino (1, 2), Baolin Deng (10, 11), Mike Dodd (13), Dan Giammar (7, 8), Ray Hozalski (13), Tim Kratz (12), Doug Latch (17), Alison McKay (4, 6), Kris McNeill (17), Paige Novak (6, 15), Jerry Schnoor (15), Timm Strathmann (3, 5), Brandy Toner (14), Rich Valentine (9, 11), and Tom Voice (8, 9). Any remaining errors are the authors' responsibility, but we sincerely hope that the readers will find few or no errors. We especially thank Mike Dodd for his extensive review and suggestions for Chapter 13 and Paul Bloom and Yo Chin for their detailed reviews and input to Chapter 18.

The senior author is happy to acknowledge the role that his previous book, *Chemical Kinetics and Process Dynamics in Aquatic Systems* (CRC Press, 1994), played in informing the writing of Chapters 5 and 17 and parts of Chapters 13 and 15. He also expresses his thanks to the students in his 2008 and 2009 water chemistry classes, in which drafts of various chapters were used as the textbook, for their helpful comments and for finding many errors. Special thanks go to Mike Gracz, PhD student in Geology and Geophysics, for his detailed reviews of the chapters. The junior author hopes that students in his future water chemistry classes do not find any errors.

Several individuals were helpful in supplying data used in this book. We are pleased to acknowledge Larry Baker, Joe Delfino, Paul Chadik, Charles Goldman, Patricia Arneson, and Ed Lowe for chemistry data used in Chapter 2; Tim Kratz and Jerry Schnoor for dissolved oxygen data used in Chapter 12; Rose Cory for fluorescence spectra and Abdul Khwaja for NMR spectra in Chapter 18; and Dan Giammar and Mike Dodd for some of the problems at the ends of several chapters. Thanks also to Kevin Drees and Bethany Brinkman for helping the authors collect additional data used in Chapters 2 and 18. We thank Mike Evans, graduate student in Computer Science and Engineering at the University of Minnesota, for developing a user-friendly interface to the kinetic program Acuchem, and Randal Barnes for advice on solving problems using spreadsheets.

We happily acknowledge the excellent library system of the University of Minnesota and the inventors of Internet search engines, which greatly facilitated our library research and hunts for references, enabling us to continue this work wherever we could find an Internet connection.

The senior author thanks the Department of Civil Engineering and his environmental engineering colleagues at the University of Minnesota for a light teaching load

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over the past few years, which enabled him to focus his time and efforts on writing the book. The junior author wishes he had the same luxury, but he still managed to squeeze in a fair bit of writing. Both authors thank their colleagues and especially their families for their understanding and patience when the writing absorbed their time.

Finally, we acknowledge with gratitude our predecessors in writing water chemistry books, starting with Werner Stumm and James J. Morgan and extending to more recent authors: Mark Benjamin, Philip Gschwend, Janet Hering, Dieter Imboden, David Jenkins, James Jensen, Francois Morel, James Pankow, Rene Schwarzenbach, Vernon Snoeyink, and others, on whose scholarly efforts our own writing has relied, and the countless researchers, only some of whom are cited in the following pages, responsible for developing the knowledge base that now enriches the field of environmental water chemistry.

# **Symbols and Acronyms**

# **Symbols**

 $a_i$ ,  $a_i$  activity of i

size parameter for ion i in Debye-Hückel equation

[]	mass or molar concentration
{}	activity
$\equiv M$	metal center attached to a solid surface
$\equiv S$	surface site
<b>‰</b>	parts per thousand (per mil)
$\boldsymbol{\alpha}_i$	fraction of $X_T$ present as species i
$\alpha_{\lambda}$	beam attenuation coefficient of light at wavelength $\boldsymbol{\lambda}$
$\alpha_{\mathrm{D}\lambda}$	diffuse attenuation coefficient of light at wavelength $\lambda$ (also $K_{\lambda})$
β	buffering capacity (chapter 8)
β	cumulative stability (formation) constant (chapter 9)
β	Bunsen coefficient (chapter 18)
γ	activity coefficient
$\gamma_{\pm}$	mean ionic activity coefficient of a salt
γ	interfacial energy or surface tension (chapters 3, 12)
Θ	temperature coefficient in kinetics
$\theta_{\scriptscriptstyle A}$	fraction of binding sites occupied by sorbate A (chapter 12)
$\epsilon_{\lambda}$	molar absorptivity (wavelength dependent)
κ	transmission coefficient (chapter 5 only)
$\kappa^{-1}$	radius of ionic atmosphere (Debye parameter), and characteristic thickness of th
	electrical double layer
κ	$\log K_{\rm a}$ (chapter 20)
λ	wavelength
μ	chemical potential
ν	stoichiometric coefficient
ν	kinematic viscosity (m <sup>2</sup> s <sup>-1</sup> ) (chapter 18)
$\nu_{\rm f}$	fundamental frequency factor
ξ	extent of reaction
ρ	density
ρ	susceptibility factor (chapter 13)
$\rho_{\rm w}$	flushing coefficient for water in a reactor (= $Q/V$ )
σ	Hammett constant
τ	characteristic time
Φ	quantum yield
$\Psi_{0}$	electrostatic surface potential
Ω	saturation ratio for mineral salts (chapter 10)
ω	electrostatic interaction factor
$a_{\lambda}$	light absorption coefficient at wavelength λ

#### xx Symbols and Acronyms

ionic strength

Α pre-exponential or frequency factor in Arrhenius equation atomic weight at. wt. at. no. atomic number boiling point b.p. c, C concentration С correction factor (chapter 13) C(electrical) capacitance (Chapter 12)  $C_p$ heat capacity change in heat capacity for a reaction  $\Delta C_p$ wavelength-dependent distribution function for scattered light (chapter 14)  $D_{\lambda}$ D diffusion coefficient D distribution coefficient (chapter 13) D dielectric constant (relative static permittivity)  $D_{\circ}$ permittivity in a vacuum observed distribution coefficient (chapter 4)  $D_{obs}$ thermodynamic distribution coefficient (chapter 4) Da daltons (molecular weight units) ΛE change in internal energy type of molecular orbital  $e_{\rm g}$ a hydrated electron  $e_{aq}^{-}$ scalar irradiance at depth z (chapter 14)  $E_{0\lambda,z}$ electrical (reduction) potential under standard conditions oxidation-reduction potential measured on the hydrogen scale Ен  $E_{act}$ energy of activation band gap energy  $E_{bg}$ scalar irradiance just below the water surface (also  $Z_{\lambda}$ )  $E_{0\lambda,0}$ esu electrostatic units fraction of a substance in a specific phase (chapter 13) f fugacity of substance i  $f_{i}$  $f_{i}$ fragment constants for fragment i (chapter 13) fraction of organic carbon  $f_{oc}$ F Helmholtz free energy F Faraday, unit of capacitance (chapter 12) Gran function (used in alkalinity titrations) F, F Faraday's constant G Gibbs free energy  $\Delta_f G^{\circ}$ free energy of formation under standard conditions  $\Delta .G^{\circ}$ change in free energy (or free energy of reaction under standard conditions) ΔG≠ free energy of activation Planck's constant Н enthalpy  $\Delta_{f}H^{\circ}$ enthalpy of formation under standard conditions  $\Delta$ , $H^{\circ}$ change in enthalpy of reaction under standard conditions Henry's law constant (=  $K_{\rm H}^{-1}$ ) Н current  $i_0$ exchange current

 $I_{\scriptscriptstyle{a\lambda}}$ (wavelength-dependent) number of photons absorbed per unit time total irradiance (wavelength-dependent)  $I_{\alpha}$ direct irradiance corrected for reflection (wavelength-dependent)  $I_{d\lambda}$ sky irradiance corrected for reflection (wavelength-dependent) I. joule kPa kilopascals (unit of pressure) k Boltzmann constant (gas constant per molecule) k, molar compressibility of i k rate constant specific light absorption rate constant (usually summed over wavelength range)  $k_{\alpha\lambda}$ direct photolysis rate constant (usually summed over wavelength range)  $k_{\mathrm{d}\lambda}$ diffuse attenuation coefficient of light at wavelength  $\lambda$  (also  $\alpha_{D\lambda}$ ) K or aK thermodynamic equilibrium constant (products and reactants expressed in terms of activity)  $^{c}K$ equilibrium constant expressed in terms of concentrations of products and reactants  $K_{aw}$ air-water partition coefficient  $K_{d}$ solid-water partition coefficient Henry's law coefficient (=  $H^{-1}$ )  $K_{H}$ gas transfer coefficient (units of length time-1)  $K_{\scriptscriptstyle \rm I}$ Langmuir sorption constant  $K_{r}$ organic carbon-water coefficient  $K_{oc}$  $K_{ow}$ octanol-water partition coefficient ion product of water  $K_{\omega}$  $l_{\lambda}$ (light path) length ultimate (first-stage) biochemical oxygen demand molal concentration m M molar concentration total mass  $M_{T}$ m/zmass-to-charge ratio number (of molecules, atoms, or molecular fragments) nuclophilicity constant (chapter 13) n N normality (equivalents/L) probability function for equilibrium constant KN(K)Avogadro's number  $N_{\scriptscriptstyle \Delta}$ negative logarithm of relative electron activity; a measure of the free energy of рε electron transfer, pronounced "pea epsilon" pН negative logarithm of hydrogen ion activity pH of point of zero charge on surfaces  $pH_{PZC}$ pH of zero net proton charge  $pH_{ZNPC}$ pΧ negative logarithm of X Р pressure p primary production (chapter 18) q charge density in diffuse layer (chapter 12) q 0 hydraulic flow rate ratio of peak areas determined via gas chromatography r

R

gas constant

#### xxii Symbols and Acronyms

R respiration (chapter 18)

R<sup>2</sup> coefficient of determination (statistical measure)

R rate

s substrate constant (chapter 13)

 $s_{\lambda} \hspace{1cm} \text{wavelength-dependent light-scattering coefficient (subscripts f or b indicate forward}$ 

or back scattering)

 $s_{\lambda}$  spectral slope over wavelength range  $\lambda_1$  to  $\lambda_2$  (in nm) (Chapter 20)

S entropy

S saturation ratio

Sc dimensionless Schmidt number (kinematic viscosity/diffusion coefficient)

 $S_r$  slope ratio (ratio of  $s_{275-295}$  to  $s_{350-400}$ )

 $t_{2g}$  type of molecular orbital

t, half-life

t<sub>c</sub> critical time (time to achieve maximum DO deficit in Streeter-Phelps model)

T temperature

TOTX total concentration of X in all phases of a system

 $U_{10}$  wind velocity 10 m above the surface

V volume

V°, standard molar volume for i

w, W work

 $W_{\lambda}$  sum of direct  $(I_{d\lambda})$  and sky  $(I_{s\lambda})$  irradiance corrected for reflection (wavelength-dependent)

 $X_T$  total concentration of all species of X in solution

X<sub>max</sub> maximum sorption capacity

y amount of O<sub>2</sub> consumed at any time in biochemical oxygen demand test

z charge (on an ion) z depth (chapter 14)

 $z_{pz}$  depth of photic zone (chapter 14)  $Z_{AB}$  collision frequency between A and B

 $Z_{\lambda}$  scalar irradiance just below the water surface (also  $E_{0\lambda,0}$ )

### **Acronyms**

2,4-D 2,4-dichlorophenoxyacetic acid

AAS atomic absorption spectrophotometry

ACD Ahrland-Chatt-Davies classification system

ACP actual concentration product

ACT activated complex theory
AHM aquatic humic matter

AIC Akaike information criterion

ANC acid-neutralizing capacity (= alkalinity)

AOP advanced oxidation process

APase alkaline phosphatase BCF bioconcentration factor

BET Brunauer-Emmet-Teller sorption equation

BLM biotic ligand model

BNC base neutralizing capacity
BOD biochemical oxygen demand
BSM basic Stern model (Chapter 12)

BTEX benzene, toluene, ethylbenzene, and xylene

CAS Chemical Abstract Service

CB conduction band

CCM constant capacitance model

CD-MUSIC charge distribution multi-site complexation (model)

CFSTR continuous-flow stirred tank reactor
cgs centimeter-gram-second, system of measure
CDOM colored (or chromophoric) dissolved organic matter

CH carbonate hardness

CLE-ACSV competitive ligand equilibration-adsorptive cathodic stripping

voltammetry

CNT carbon nanotube

COD chemical oxygen demand

CP-MAS NMR cross-polarization-magic angle spinning nuclear magnetic resonance

(spectroscopy)

CPU chloroplatinate unit

CRAM carboxyl-rich alicyclic material

CUAHSI Consortium of Universities for the Advancement of Hydrologic Science, Inc.

DAX resin material used to extract AHM from water

DBE double bond equivalents

DBE/C double bond equivalents per carbon atom

DBP disinfection by-product DCE dichloroethylene

DDT dichlorodiphenyltrichloroethane
DEAE diethylaminoethyl (functional group)

DFAA dissolved free amino acid
DHLL Debye-Hückel limiting law
DIC dissolved inorganic carbon

DLM double-layer model
DMF 2,5-dimethylfuran
DMG dimethylglyoxime
DO dissolved oxygen

DOC dissolved organic carbon
DOM dissolved organic matter
DON dissolved organic nitrogen
DOP dissolved organic phosphorus
DRP dissolved reactive phosphate

E2/E3 ratio of absorbance at 250 nm to absorbance at 365 nm E4/E6 ratio of absorbance at 465 nm to absorbance at 665 nm

EAC electron accepting capacity (Chapter 20)

EAWAG German acronym for Swiss Federal Institute of Aquatic Science and

Technology

EDC electron donating capacity (Chapter 20)
EDHE extended Debye-Hückel equation

#### xxiv Symbols and Acronyms

EDTA ethylenediaminetetraacetic acid EEM(s) excitation-emission matrix (matrices)

EfOM effluent organic matter

EPC equilibrium phosphorus concentration
EPICS equilibrium partitioning in closed systems
EPI Suite Estimation Programs Interface Suite

EPR electron paramagnetic resonance (spectroscopy)
EXAFS extended x-ray absorption fine structure spectroscopy

FA fulvic acid

fDOM fluorescent dissolved organic matter

FFA furfuryl alcohol FI fluorescence index

FITEQL nonlinear data fitting program

FT-ICR MS Fourier transform ion cyclotron resonance mass spectrometry

GC-MS gas chromatography-mass spectrometry

GCSOLAR public domain computer program to calculate light intensity and rates of

direct photolysis

HA humic acid HAA haloacetic acid HAc acetic acid

HFO two-layer surface complexation model for ferrihydrite HMWDON high-molecular-weight dissolved organic nitrogen

HOMO highest occupied molecular orbital

HPLC high-performance liquid chromatography
HRMS high resolution mass spectrometry

HRT hydraulic residence time

HSAB (Pearson) hard-soft acid-base (system)

IAG internal alkalinity generation

IAP ion activity product
IC ion chromatography
ICP inductively coupled plasma

IEP isoelectric point

IHSS International Humic Substances Society

IMDA imidodiacetic acid IP inositol phosphate

IR infrared

is inner sphere (complex)

IUPAC International Union of Pure and Applied Chemistry

LC-MS liquid chromatography-mass spectrometry

LED light-emitting diode

LFER linear free energy relationship

LMCT ligand-to-metal charge transfer (process)

LULC land use-land cover

LUMO lowest unoccupied molecular orbital

MCL maximum contaminant level

MDF mass dependent fractionation (Chapter 16)

MEMS microelectromechanical system

MER/MEO mediated electrochemical reduction/oxidation (Chapter 20)

MIF mass independent fractionation (Chapter 16)
MINEQL computer program to calculate mineral equilibria
MINEQL+ commercially available equilibrium computer program

MW molecular weight

NADP National Atmospheric Deposition Program

NCH noncarbonate hardness NDMA N-nitrosodimethylamine

NICA-Donnan non-ideal competitive adsorption-Donnan (model)

NMR nuclear magnetic resonance (spectroscopy)

NOM natural organic matter

<sup>3</sup>NOM<sup>\*</sup> triplet excited state natural organic matter

NP nanoparticle NTA nitrilotriacetic acid

NTU nephelometric turbidity unit os outer sphere (complex)

PAH polycyclic aromatic hydrocarbon

PARAFAC parallel factor analysis; technique to evaluate DOM quality from

fluorescence spectra (EEMs)

PBDE polybrominated diphenylether PCB polychlorinated biphenyl

PCDD/Fs polychlorinated dibenzodioxins/furans
PCE perchloroethylene or tetrachloroethylene
PCU platinum-cobalt color unit (Hazen unit)

PES potential energy surface
PFOA perfluorooctanoic acid
PFOS perfluorooctane sulfonic acid

PFR plug-flow reactor

PON particulate organic nitrogen POP persistent organic pollutant PP particulate phosphorus

PPC products of proton consumption

PPCPs pharmaceutical and personal care products

PPR products of proton release

PPRI photochemically produced reactive intermediate

PSU practical salinity unit ROS reactive oxygen species

RPHPLC reverse-phase high-performance liquid chromatography

S salinity

SC specific conductance SCM surface complexation model

SD standard deviation

SEC size-exclusion chromatography

SII specific ion interaction

SMILES Simplified Molecular Input Line Entry System

#### xxvi Symbols and Acronyms

SMOW standard mean ocean water
SMP soluble microbial products
SRFA Suwannee River fulvic acid
SRHA Suwannee River humic acid

SRP soluble reactive phosphate (expressed as P)

STP standard temperature and pressure SUVA specific ultraviolet absorption SWCNT single-walled carbon nanotube

TCE trichloroethylene
TCP 2,4,6-trichlorophenol
TDP total dissolved phosphorus
TDS total dissolved solids
TH total hardness

THM trihalomethane

ThOC threshold odor concentration

TLM triple-layer model
TMA trimethylamine
TNT trinitrotoluene
TOC total organic carbon
TON total organic nitrogen
TP total phosphorus
TST transition state theory

UF ultrafiltration

U.S. EPA U.S. Environmental Protection Agency

USGS U.S. Geological Survey

UV ultraviolet VB valence band

VMINTEQ Visual MINTEQ (public domain equilibrium program based on

MINEQL)

VOC volatile organic compound

WHAM Windermere humic acid model (public domain computer program) for

metal binding to AHM; ver. 6 (2002) is the latest version

WWTP wastewater treatment plant

XAD see DAX

XANES x-ray absorption near-edge spectroscopy

# **Units for physical quantities**

Fundamental quantities		Some derived	Some derived quantities		
Quantity	SI units	Quantity	SI units		
Length	meter, m	Force	newton (kg·m·s <sup>-2</sup> )		
Mass	kilogram, kg	Volume	cubic meters $(m^3)^*$		
Time	second, s	Electric charge	coulomb, $C = A \cdot s$		
Electric current	ampere, A	Power	watt, $W = J \cdot s^{-1}$		
Temperature	Kelvin, K	Electric potential	volt, $V = W \cdot A^{-1}$		
Amount of material	mole, mol	Electric resistance	ohm, $\Omega = V \cdot A^{-1}$		
		Conductance	Siemens, $S = A \cdot V^{-1}$		

# **Important constants**

Avogadro's constant (number) $6.022 \times 10^{23} \text{ mol}^{-1}$ e (the "natural" number) $2.71828$ Electron charge $1.602 \times 10^{-19} \text{ coulombs (C) or}$ $4.803 \times 10^{-10} \text{ esu}$ Electron mass $9.109 \times 10^{-31} \text{ kg}$
Electron charge $1.602\times 10^{-19} \text{ coulombs (C) or}$ $4.803\times 10^{-10} \text{ esu}$ Electron mass $9.109\times 10^{-31} \text{ kg}$
$4.803 \times 10^{-10}  esu$ Electron mass $9.109 \times 10^{-31}  kg$
Electron mass $9.109 \times 10^{-31} \mathrm{kg}$
e e e e e e e e e e e e e e e e e e e
Fundamental frequency, $\nu$ (reciprocal $6.2 \times 10^{12}  \text{s}^{-1}$
of molecular vibration period)
Faraday, $\Im$ 96,485 C mol <sup>-1</sup>
Gas constant per mole, R $8.314  \text{J mol}^{-1}  \text{K}^{-1}  \text{or}  1.987  \text{cal mol}^{-1}  \text{K}^{-1}$
Gas constant per molecule, k, called $1.3805 \times 10^{-23} \text{J K}^{-1}$
the Boltzmann constant
Gravitation constant (of the Earth) $9.806 \text{ m s}^{-2}$
Melting point of water 0 °C or 273.15 K
Molar volume of an ideal gas at $0$ °C $22.414 \mathrm{L}\mathrm{mol}^{-1}\mathrm{or}22.414 \times 10^3\mathrm{cm}^{-3}\mathrm{mol}^{-1}$
and 1 atm
Molecular vibration period $1.5 \times 10^{-13}$ s
Permittivity of a vacuum, $\varepsilon_0$ , now $8.854 \times 10^{-12}  \text{J}^{-1}  \text{C}^2  \text{m}^{-1}$ (or Farads per meter)
called the electric constant
$\pi$ 3.14159
Planck's constant, h $6.626 \times 10^{-34} \mathrm{J}\mathrm{s}$
Relative static permittivity of 80.1 (dimensionless) at 20°C
water, <i>D</i> , also called the
dielectric constant)
Speed of light (in a vacuum), c $2.998 \times 10^8 \text{ m s}^{-1}$

 $<sup>^*</sup>$  The liter (L) is not an SI unit but is widely used as the unit of volume in freshwater studies. 1 L =  $10^{-3}$  m $^3$  = 1 dm $^3$ . Some scientific journals use SI units only and use m $^3$  for volumetric measurements.

# Conversion factors for energy-related quantities

```
1 newton (unit of force) = 1 \text{ N} = \text{kg m s}^{-2}

1 joule (unit of energy) = 10^7 \text{ erg} = 1 \text{ N m} = \text{kg m}^2 \text{ s}^{-2} = 1 \text{ volt coulomb (V C)} = 0.239

calories (cal) = 9.9 \times 10^{-3} \text{ L atm}^{-1} = 6.242 \times 10^{18} \text{ eV}

1 cal = 4.184 \text{ J}

1 watt = 1 \text{ J s}^{-1} = 1 \text{ kg m}^2 \text{ s}^{-3} = 2.39 \times 10^{-4} \text{ kcal s}^{-1} = 0.86 \text{ kcal h}^{-1}

1 entropy unit = 1 \text{ cal mol}^{-1} \text{ K}^{-1} = 4.184 \text{ J mol}^{-1} \text{ K}^{-1}
```

# **Conversion factors for pressure**

```
1~atm=760~mm~Hg=1.013\times10^5~Pa~(pascals)=101.3~kPa=1.013~bars 1~mm~Hg=1~torr 1~Pa=10^{-5}~bars=1~N~m^{-2}
```

# Some useful relationships

```
RT ln x = 2.303RT log x = 5.709 log x (kJ mol<sup>-1</sup>) = 1.364 log x (kcal mol<sup>-1</sup>) at 25 °C (298.15 K) (RT/$\frac{3}{3}$) ln x = 2.303RT/$\frac{3}{3}$ log x = 0.05916 log x (V at 25 °C, or 59.16 mV at 25 °C)
```

# PART I PROLOGUE

# **Introductory Matters**

### **Objectives and Scope**

This chapter sets the stage for the rest of the book by addressing five topics. First, a brief description of the nature and scope of water chemistry and its relationship to other environmental sciences provides context for the topics treated in this book. Second, a description of the unique properties of water and their relationship to its molecular and macroscopic structure provides an appreciation for the complexity of the medium that supports the chemistry we wish to understand. Third, the many units used to report concentrations of chemicals in water—some common, some standard chemical units, and some unique to environmental engineering and chemistry—are introduced. We show how to use them and interconvert them as a first step in analyzing the chemistry of water quantitatively. Fourth, we introduce the major types of chemical reactions that occur in natural and engineered water systems and describe the kinds of models and equations used to quantify the equilibrium conditions that they tend to approach and rates at which they occur. Finally, we provide a brief review of the origins of water chemistry and its development as a scientific discipline.

### **Key Concepts and Terms**

- The "overlapping neighborhoods" of water chemistry, marine chemistry, aqueous geochemistry, biogeochemistry, soil chemistry, and many other environmental sciences
- The unique physical-chemical properties of water
- Liquid water as a structured fluid caused by extensive hydrogen bonding to form water "clusters"
- Common mass units of concentration: parts per million (ppm) and parts per billion (ppb); milligrams per liter (mg/L) and micrograms per liter (µg/L)
- Chemical concentration units: moles/liter (molarity, M), moles/kilogram of water (molality, m), equivalents/liter, normality (N), mole fraction
- Concentration units unique to water chemistry: mg/L as CaCO<sub>3</sub>; mg/L as N, P, Cl, or other elemental components of ions and molecules
- Stoichiometric, equilibrium, and kinetic modeling approaches
- Associative reactions: acid-base, solubility (precipitation and dissolution), complex formation and dissociation
- Redox processes: oxidation as a loss of electrons; reduction as a gain in electrons

#### 4 Water Chemistry

- Sorption: a phase-transfer process
- Gas transfer and Henry's law

# 1.1 Introduction: Definition and scope of water chemistry

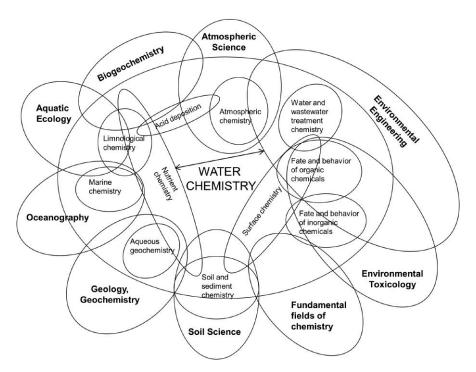
As a recognized field of science, water chemistry developed in the mid-twentieth century at the dawn of the "environmental era," but as described later in this chapter (Section 1.5), its origins go back considerably further in time. Before proceeding, it may be useful to provide a brief description of what we think the field of water chemistry comprises. Defining scientific fields in a way that is more than self-referential (i.e., "water chemistry is the chemical study of water") can be difficult because of the overlapping nature of related scientific disciplines, as illustrated in Figure 1.1. For present purposes, we propose the following description:<sup>1</sup>

Water chemistry deals with the solutes and suspended substances in natural waters and aquatic systems engineered by humans, and it focuses on the reactions and phase-transfer processes that change solute concentrations in water. The theoretical rigor of fundamental chemistry supports a broader framework for water chemistry research and practice that seeks to integrate and interpret relevant biogeochemical processes across diverse natural and engineered waters using a combination of field, laboratory (experimental), and analytical (modeling) methods. Water chemistry focuses not so much on water itself but on what is in water. The unique characteristics of water as a solvent play important roles, however, in determining the types and rates of reactions and phase-transfer processes that occur. In addition, water chemistry generally focuses on temperatures between 0 and 40 °C, pH values between 5 and 9 (with exceptions related to volcanic activity, acid rain, and hazardous wastes), and usually on relatively dilute concentrations. Finally, the broad goals of water chemistry as a discipline include improving our understanding of how chemical processes affect aquatic systems and developing techniques to improve treatment and remediation of waters impaired by human activities.

#### 1.2 Nature of water

### 1.2.1 A societal perspective

Water is by far the most common liquid on the Earth's surface, and its unique properties enable life to exist. Water is usually regarded as a public resource—a common good—because it is essential for human life and society, but too much water or water in the wrong places also is a problem: witness the extensive flooding problems caused by hurricanes and increasingly common extreme rain events. Water also is an



**Figure 1.1** Overlapping neighborhoods of the sub-fields in water chemistry and related disciplines. The size of the ovals is not intended to indicate the importance of a given sub-field or discipline, and the extent (or lack) of overlap of ovals reflects drawing limitations more than the extent of concordance among sub-fields and disciplines. In the interest of clarity, not all active and potential interactions are illustrated; the double-headed arrow shows one obvious interaction not otherwise indicated in the diagram—that between nutrient chemistry and environmental engineering and its subfield of water/wastewater treatment.

economic resource and is sold as a commodity. Water rights in the American West are continuous source of conflict<sup>2</sup> and a problem of global magnitude.<sup>3</sup> Beyond these perspectives, water holds a special place in human society and indeed is often spoken of in terms of its mystical and transcendent properties. Water has spiritual values in many cultures and is associated with birth, spiritual cleansing, and death. The fact that about 70% of the Earth's surface is covered by water and only 30% by land makes one wonder whether "Planet Earth" more properly might be named "Planet Water."

For chemists, water is a small, simple-looking, and common molecule,  $H_2O$ , but they know it has many unusual and even unique properties, as discussed below. For civil engineers, water is a fluid to be transported via pipes and channels. When it occurs in rivers and streams, it is viewed partly as an obstacle to transportation, for which bridges need to be designed and constructed, and partly as an energy-efficient means of transportation and shipping. Scientists in many other disciplines have their own viewpoints about water that reflect how it interacts with their science.

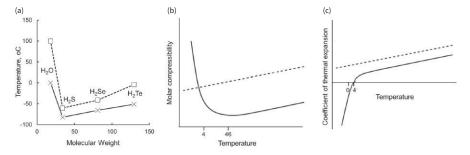
# 1.2.2 Physical properties of water

Water is the medium for all the reactions and processes that comprise the foci of this book. Here we focus on the properties of water itself, describe its molecular structure, and show how that structure leads to the macroscopic structures of liquid, solid, and gaseous water and their unusual physicochemical properties. Compared with other small molecules, water has very high melting and boiling point temperatures.<sup>4</sup>

Compound	Formula	Mol. Wt.	Freezing pt. (°C)	Boiling pt. (°C)
Methane	$CH_4$	16	-182.5	-161.5
Ammonia	$NH_3$	17	-77.7	-33.3
Water	$H_2O$	18	0	100
Carbon monoxide	CO	28	-205	-191.5
Nitric oxide	NO	30	-164	-152

Moreover, as Figure 1.2a shows, water does not follow the trend of decreasing melting and boiling points with decreasing atomic weight shown by the other Group 16 (formerly called Group VI; see Periodic Table in Chapter 2) hydrides, and it also differs from typical liquids in the temperature dependence of several other physical properties (Figure 1.2b,c).

Among common liquids, water has the highest heat capacity, heat conduction, heats of vaporization and fusion, and dielectric constant (or "relative static permittivity"); see Table 1.1. The latter characteristic measures the attenuation rate of coulombic forces in a solvent compared to attenuation in a vacuum, and it is important for



**Figure 1.2** Trends in melting point (solid line) and boiling point data<sup>4</sup> for the Group VI hydrides (a) and temperature relationships for some physical properties of water (solid line) and typical liquids (dashed line): isothermal compressibility,  $k_T$ , a measure of how pressure affects molar volume (b), and the coefficient of thermal expansion,  $\alpha_P$ , a measure related to density (c).

Parts (b)–(c) redrawn from Nilsson and Pettersson.<sup>5</sup>

Table 1.1 Physical properties of water<sup>a</sup>

Property	Value	Comparison with other liquids	Environmental Importance
State (at room temperature)	Liquid	Rather than a gas like H <sub>2</sub> S and H <sub>2</sub> Se	Provides medium for life
Heat capacity Specific heat	1.0 cal g <sup>-1</sup> °C <sup>-1</sup> 4.18 J g <sup>-1</sup> °C <sup>-1</sup>	Very high	Moderates climate
Latent heat of fusion	79 cal/g 330 J/g	Very high	Moderating effect; stabilizes air temperatures
Latent heat of evaporation	540 cal/g 2257 J/g	Very high	Moderating effect; important in hydrology for precipitation–evaporation balances
Density at 4 °C	1.0 g/cm <sup>3</sup>	High; anomalous maximum at 4 °C	Causes freezing to occur from air-water surface; controls temperature distribution and water circulation in lakes and oceans
Surface tension at 20 °C	72.8 dyne/cm 72.8 mN/m	Very high	Affects adsorption, wetting, and transport across membranes
Dielectric constant <sup>b</sup>	80.1 at 20 °C (dimensionless)	Very high	Makes water a good solvent for ions; shields electric fields of ions
Dipole Moment	1.85 debyes	High compared with organic liquids	Cause of above characteristics and solvent properties of water
Viscosity	$1.0 \times 10^{-3} \mathrm{Pa \cdot s}$ 1 centipoise (cP) at 20 °C	2–8× higher than organic liquids	Slows movement of solutes
Transparency	High	Especially in mid-visible range	Allows thick zone for photosynthesis and photochemistry
Thermal conductivity	$0.6~{\rm W}~{\rm m}^{-1}~{\rm K}^{-1}$	High compared with organic liquids	Critical for heat transfer in natural and engineered systems

<sup>&</sup>lt;sup>a</sup> Adapted from Horne.<sup>6</sup>

the dissolution of salts in water. Compared to solvents with low dielectric constants, the high dielectric constant of water permits like-charged ions to approach each other more closely before repulsive coulombic forces become important. Consequently, it is a key property enabling water to be such a good solvent for salts.

In general, the unusual physical properties of liquid water reflect the fact that water molecules do not behave independently but are attracted to each other and to many solutes by moderately strong "hydrogen bonds." The bond strengths of the

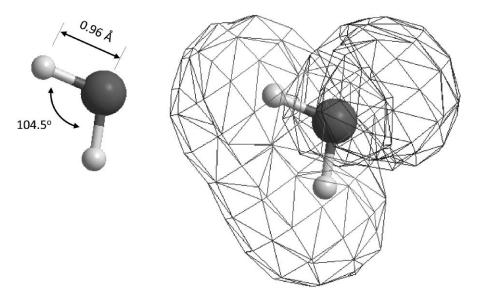
<sup>&</sup>lt;sup>b</sup> Also called relative static permittivity.

#### 8 Water Chemistry

hydrogen bonds in ice and liquid water, ~21 kJ/mol,<sup>6</sup> are much weaker than the O–H bond of water 464 kJ/mol but stronger than London-van der Waals forces (<4 kJ/mol). In addition, the hydrogen bonds in water are stronger than those in NH<sub>3</sub> (13 kJ/mol) but much weaker than those in HF (155 kJ/mol). The differences in H-bonding strengths among these molecules is explained in terms of the electronegativity of the non-H atom. The importance of hydrogen bonding in promoting structure in ice and liquid water is enhanced by the fact that H<sub>2</sub>O has two hydrogen atoms and two pairs of electrons on the oxygen, thus allowing each water molecule to have a potential of four hydrogen bonds. In contrast, each HF can have only three bonds (because each HF has only one hydrogen atom). The importance of hydrogen bonding in NH<sub>3</sub> is lessened by the fact that the N atom has only one pair of electrons available to form such a bond.

#### 1.2.3 Basic structural features of water

Hydrogen bonding is a consequence of the basic molecular structure of water. The angle between the two O–H bonds (105°) in water is greater than the 90° expected for perpendicular p-orbitals (Figure 1.3). This is caused by repulsion between the hydrogen atoms and indicates that there is some hybridization of the s and p orbitals in the electron shell of the O atom. Oxygen's four remaining valence electrons occupy two orbitals opposite the hydrogen atoms in a distorted cube arrangement.



**Figure 1.3** H–O bond angle and lengths in the  $H_2O$  molecule (left) lead to high polarity of the molecule with the hydrogen atoms (right: positive, red mesh) on the left side and the unshared electron pairs (right: negative, blue [darker gray] mesh) on the right side. (See color insert at end of book for a color version of this figure.)

This explains the molecule's large dipole moment. The electron pairs attract hydrogen atoms of adjacent water molecules and form hydrogen bonds with lengths of 1.74 angstroms (Å; measured in ice by X-ray diffraction), which leads to the threedimensional structure found in ice and liquid water.

The structure of ice is known with great accuracy.<sup>6</sup> Ice-I<sub>h</sub>, the form that occurs under environmental conditions, has a structure in which each water molecule is surrounded by the oxygen atoms of four adjacent water molecules in a tetrahedral arrangement (Figure 1.4). Extending this arrangement in three dimensions gives rise to a fairly open (i.e., low-density) crystalline structure of repeating hexagonal rings (hence the subscript h in I<sub>h</sub>), each of which contains six water molecules. The density of ice calculated from measured bond lengths and the three-dimensional structure agree with the measured density of ice.

In contrast to the rigid crystalline structure of ice, gaseous water has no structure beyond that of the individual molecules themselves except for occasional, ephemeral dimers. In the gas phase, each water molecule behaves independently, and, when two water molecules collide, they do not stick together but simply bounce off each other and continue their independent existences.

The degree of structure in liquid water is intermediate between crystalline ice and unstructured gaseous water. Models of the structure of water must account for the properties in Table 1.1, which suggest that water is a structured medium. The model must also explain the variations in these properties with temperature,

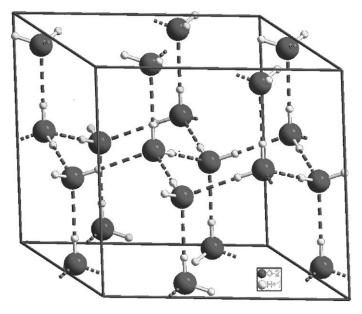


Figure 1.4 Tetrahedral arrangement of hydrogen-bonded water molecules in ice leads to an open hexagonal ring structure in crystalline ice-I  $_{\rm h}.$  (See color insert at end of book for a color version of this figure.)

Source: Wikimedia Commons, file Hex ice.GIF (public domain).

the higher density of water than ice, and the density maximum at 4 °C. The heat of fusion of ice (330 J/g)—the energy required to convert ice at 0 °C to liquid water at 0 °C —suggests that only ~15% of the hydrogen bonds in ice are lost upon melting. In addition, studies using a variety of methods have reported that the average molecule in liquid water participates in 2.2–3.6 H-bonds. The structure of water has been a subject of inquiry for many decades. Proposed models include a "relic ice" model and another in which water molecules exist in a clathrate or cage-like structure.  $^6$ 

The so-called *flickering-cluster model* described by Frank and Wen<sup>7</sup> in 1957 was regarded for many decades as a reasonable if not exact description for the structure of liquid water. According to this model, water molecules form clusters of H-bonded molecules of indeterminate structure (Figure 1.5). The clusters have very short lives ( $\sim 10^{-10}$  s) and are constantly forming and disintegrating with thermal fluctuations at the microscale. Although the lifetime of clusters may seem trivially short, it is about a thousand times longer than the time between molecular vibrations ( $\sim 10^{-13}$  s), and clusters thus have a real, if very ephemeral, existence. Because of dipole effects on individual water molecules, the formation of hydrogen bonds is a cooperative phenomenon, and formation of one bond facilitates formation of the next. Consequently, rather large clusters are formed. The average cluster has 65 molecules at 0 °C but only 12 at 100 °C. Nonetheless, because the number of

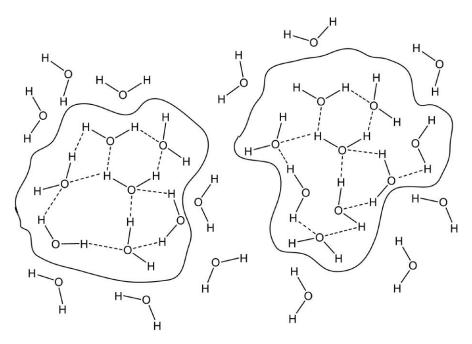


Figure 1.5 The flickering cluster model of liquid water.

clusters increases with temperature, the fraction of molecules in clusters decreases much more slowly (from ~75% at 0 °C to ~56% at 100 °C).6 Unclustered water is considered to be "free."

# 1.2.4 Advanced topic: Dynamic structure of liquid water

Although the large-scale structure of water was not specified by the Frank-Wen model, the anomalous properties of water are thought to arise from a competition between the relatively bulky way of connecting molecules via the ideal tetrahedral angles arising from the molecular structure of water and more compact arrangements that have more bond strain and broken bonds. The alternatives provide a continuum of structural possibilities, but some can be ruled out by experimental evidence. For example, if the clusters were relic ice structures, the polygons formed by H-bonding would reflect the hexagonal structure of ice and contain an even number of molecules. Breaking a hydrogen bond in hexagonal ice-I<sub>b</sub> yields a 10-membered ring; loss of a second H-bond yields a 14-membered ring. The frequency distribution of polygon sizes in water shows no evidence8 for relic ice structures, however, and the most common polygons found in molecular dynamics simulations are five-member rings that are not possible products of ice-I<sub>b</sub>.

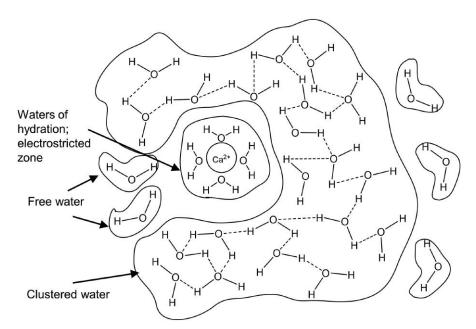
Many refinements in our understanding of the complicated, dynamic structure of liquid water have been made over the past 20 years using molecular dynamics modeling<sup>9</sup> and sophisticated experimental methods, such as femtosecond infrared (IR) spectroscopy and X-ray emission and absorption, and Raman scattering spectroscopy. 5,10 Although the highly ephemeral nature of water's structure inherent in the Frank-Wen model still is valid, the term "flickering cluster" is no longer in vogue in chemical physics. In addition, molecular dynamics simulations indicate that the lifetime of individual water clusters is not a single value but varies over a wide range:  $\sim 10^{-13}$  to  $10^{-9}$  s.<sup>11</sup>

Recent models suggest that at ambient temperatures most water molecules favor a closer packing than tetrahedral, with strongly distorted H-bonds and some tetrahedrally bonded water patches occurring as fluctuations. The fraction of molecules in tetrahedral structures and size of the tetrahedral patches decreases with increasing temperature. Recent studies also suggest less extensive H-bonding occurs in liquid water than previously thought. Earlier molecular dynamics simulations predicted ~3.3-3.6 H-bonds per water molecule, which agrees with estimates based on the low heat of fusion of ice. Recent studies suggest an average of  $2.2 \pm 0.5$  H-bonds (one donating and one accepting) per water molecule at 25 °C and  $2.1 \pm 0.5$  bonds at 90 °C. The smaller number of H-bonds was reconciled with the small heat of fusion of ice by quantum mechanical calculations, indicating that H-bonds in the proposed configuration are stronger than those in the tetrahedral

ice configuration, with the net effect being only a small change in energy in spite of the larger number of broken H-bonds in liquid water. In spite of these advances, little is known about the structure of liquid water at the "nanoscale"—that is, the scale of hundreds to a few thousand water molecules. The last word has not yet been written on this topic.

# 1.2.5 Effects of solutes and surfaces on the structure of liquid water

Addition of solutes to pure water distorts its structure. The nature of the interactions between solutes and solvent water depends on whether the solute is a cation, anion, or nonelectrolyte. Solvation of cations results in relatively tight binding of water molecules in the "primary sphere of hydration" (Figure 1.6). Water molecules in the hydration sphere no longer act as solvent molecules, and tight binding results in a loss of volume compared to water in the bulk solvent; this phenomenon is known as *electrostriction*. In some models, unstructured transition zones exist between hydrated ions and the clustered water in the rest of the solvent. In contrast to cations, anions are not solvated and instead occupy interstices or "holes" in the overall solvent structure. Changes in viscosity upon addition of salts to water are used to infer changes

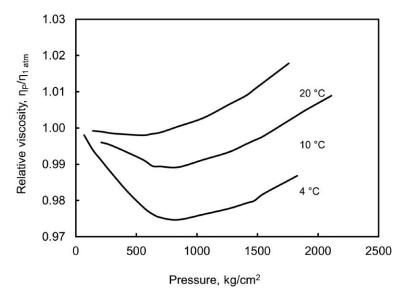


**Figure 1.6** Cation hydration leads to an "electrostricted zone" surrounded by clustered and free water.

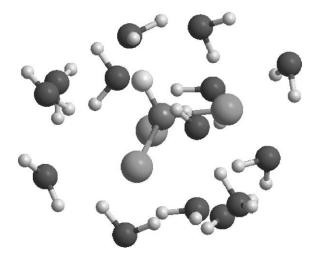
in the degree of solvent structure. Most salts are "structure-makers"—they increase viscosity—but a few salts (e.g., KCl and CaSO<sub>4</sub>) are structure-breakers that decrease viscosity. The viscosity of pure water<sup>12</sup> (Figure 1.7) and aqueous salt solutions<sup>13</sup> generally decreases with increasing pressure, reaching a minimum value at pressures of ~400–800 kg/cm<sup>2</sup> (depending on salt content and temperature), and viscosity then increases if pressure continues to increase. Horne<sup>6</sup> explained this phenomenon as a result of a breakdown in the cluster structure of water as pressure increases, such that unclustered water molecules are arranged more compactly than those in the cluster state. Once the cluster structure is lost—at the viscosity minimum—further increases in pressure pack the water molecules more tightly, and viscosity increases because of increasing friction as the molecules move past each other.

Nonpolar solutes also reside in the interstices between water clusters (Figure 1.8), with water molecules surrounding the solute maintaining their H-bonds. <sup>14</sup> Overall, this promotes structure in liquid water and limits the freedom of the organic molecule as well. <sup>15</sup> Consequently, nonpolar solutes have high negative entropies of solution (see Chapter 3 for a description of the concept of entropy).

Water molecules at the air-water interface all are oriented with the oxygen atoms facing the interface with air and the hydrogen atoms facing the solution (Figure 1.9). This distorts the three-dimensional structure of clustered water in the bulk solution, and, as a result, the interfacial region has somewhat different physical properties from bulk water. The highly ordered arrangement of water molecules at the air-water interface also explains the high surface tension of water;



**Figure 1.7** Relative viscosity of pure water versus pressure. Drawn from data in Horne and Johnson.<sup>12</sup>



**Figure 1.8** Structure of an organic (nonpolar) solute, chloroform, in liquid  $H_2O$  computed by energy minimization with MM2 force field in ChemBio3D Ultra 12.0. (See color insert at end of book for a color version of this figure.)

**Figure 1.9** The structure of liquid water is perturbed near interfaces, as the O atoms orient toward the interface.

surface tension defines the energy needed to break the surface. An analogous situation occurs at solid–water interfaces. Water in the first few molecular layers from a solid–water interface has different physical properties (e.g., a low dielectric constant) than the bulk solution. This has important implications for solute behavior at interfaces, as discussed in Chapter 12.

#### 1.3 Concentration units

### 1.3.1 Introduction

Various units are used to express concentrations of substances dissolved or suspended in natural waters. This reflects the diversity of substances in these systems, the wide range of concentrations at which they are found, and the multidisciplinary origins of water chemistry. An important first step in studying the chemistry of natural waters is to learn about the different concentration units and how they are related to each other.

In general, concentrations of substances in water are expressed in two principal ways: mass per unit volume of solution and mass per unit mass of water. Mass/volume units more accurately reflect the way we prepare and analyze solutions (i.e., based on a certain volume of solution rather than a certain weight), but they have the disadvantage of being slightly temperature dependent because the density (mass per volume) of water varies with temperature. In contrast, mass/ mass concentrations are temperature invariant. For accurate work one should express mass/volume concentrations at a standard temperature, but for routine purposes, the differences caused by temperature are usually ignored. Volumetric glassware is calibrated to contain the nominal volume at 20 °C. In either mass/ volume or mass/mass units, the mass of solutes and water may be expressed in common units (normally metric or SI units, although English units still are sometimes used in water and wastewater treatment chemistry) or chemical units, as described in the following sections.

#### 1.3.2 Common units of concentration

Both mass per unit volume of solution (mass/volume) and mass per unit mass of solvent (mass/mass) are used widely, often interchangeably, to express concentrations of dissolved and suspended substances in water (Table 1.2). For major ions in freshwater, the most convenient mass/volume unit is mg/L because major ions generally occur in the range of a few to a few hundred mg/L. The corresponding mass/mass unit is parts per million (ppm; mg/kg). For practical purposes, the terms are interchangeable for freshwater because 1 mg =  $10^{-3}$  g and 1 liter of water =  $1 \text{ kg} = 10^3 \text{ g}$  (for solutions in other solvents, see Example 1.1). Thus, we can write

1 mg of substance in 1 L of water  $\times$  1 L water/1 kg water = 1 mg substance/1 kg water

Nanogram/L

Picogram/L

Femtogram/L

Mass/volume Symbol Multiple Equivalent Substances for mass/mass unita which units are used of g Gram/liter g/L 1 Part per thousand, Major ions in brackish ppt (‰) water and seawater Milligram/L  $10^{-3}$ mg/L Part per million, ppm Major ions in freshwater  $10^{-6}$ Part per billion, ppb Microgram/L μg/L Nutrients, minor and trace metals, many organic contaminants

Part per trillion<sup>b</sup>

Trace organic pollutants

Ultratrace contaminants.

e.g., methylmercury

Not commonly used

and some trace metals

**Table 1.2** Common concentration units used in water analysis

 $10^{-9}$ 

 $10^{-12}$ 

 $10^{-15}$ 

ng/L

pg/L

fg/L

Not used

Not used

This assumes that the dissolved substance does not affect the density of the water or contribute a significant amount to the total mass. If that were the case, the equivalency of mg/L and ppm no longer would hold. The salt content of seawater is sufficiently high (range of g/L) for there to be a slight difference between concentrations expressed in g/L of solution and concentrations expressed in parts per thousand, which are often written as the "per mil" symbol, %. The differences become even more pronounced in hypersaline waters (see Example 1.2). Many substances of interest in aquatic systems occur at concentrations much less than 1 mg/L, although the major ions in seawater and brines occur at much greater concentrations. Consequently, a series of concentration units are used, as shown in Table 1.2. Also, as analytical capabilities have enhanced our ability to detect and measure increasingly lower concentrations of inorganic and organic ions and compounds in water, use of mass/volume units with the prefixes micro-, nano-, and pico- have become increasingly common. Mass/mass units generally are not used for concentrations of trace and ultratrace contaminants. Because of ambiguities associated with such terms as trillion, quadrillion, and even billion, their use in expressing concentrations should be avoided.\*

<sup>&</sup>lt;sup>a</sup> This direct conversion is possible only because the density of water is 1, and so 1 L = 1 kg. This direct relationship does not hold for other solvents.

b To avoid ambiguity, the abbreviation "ppt" should not be used; ppt is used for parts per thousand by marine scientists.

<sup>\*</sup> A "billion" in the United States is a thousand million (109), but a billion in Europe is a million million (1012).

## Example 1.1 Conversion between mass/volume and mass/mass units

You have 1 ppb standards of the pesticide alachlor in water and in hexane ( $\rho = 0.66$ g/mL). What is concentration of each standard in µg/L?

Answer: For water, the answer is straightforward:

$$1 \text{ ppb} = \frac{1 \text{ } \mu \text{g alachor}}{\text{kg water}} \times \frac{1 \text{ kg water}}{1 \text{ L water}} = \frac{1 \text{ } \mu \text{g alachor}}{\text{L water}}.$$

For hexane, the density alters the answer:

1 ppb = 
$$\frac{1 \mu g \text{ alachor}}{\text{kg hexane}} \times \frac{0.66 \text{ kg hexane}}{1 \text{ L hexane}} = \frac{0.66 \mu g \text{ alachor}}{\text{L hexane}}.$$

#### 1.3.3 Chemical units

Use of chemical units to express solute concentrations is becoming more widespread in aquatic sciences, especially in limnology, oceanography, and geochemistry, but also in environmental engineering. The fundamental mass/volume unit is molarity (moles of solute per liter of solution), abbreviated mol/L or M (but never M/L):

$$\begin{aligned} \textit{Molarity}\left(\mathbf{M}\right) &= \frac{\textit{grams of solute}}{\textit{gram formula wt.}\left(\mathbf{g/mol}\right) \times \textit{vol. of solution}\left(\mathbf{L}\right)} \\ &= \frac{\textit{grams of solute}}{\textit{vol. of solution}\left(\mathbf{L}\right)} \times \frac{1}{\textit{gram formula wt.}\left(\mathbf{g/mol}\right)}. \end{aligned}$$

Major ions in fresh water generally are in the millimolar and submillimolar (mM) range; minor constituents and nutrients generally are in the micromolar (µM) range. Nutrients in water quality typically refer to N and P. N is usually in the range of the other major ions (mM range). P is much less (µM range).

A mole of a substance is simply a defined quantity or number of units of the substance, specifically  $6.022 \times 10^{23}$  units of the substance, based on the number of atoms in exactly 12 grams of carbon-12 ( $^{12}$ C). This number is given the symbol  $N_A$  and is called Avogadro's constant (see Box 1.1). The term "mole" is used mostly with reference to molecules (and ions), and a mole of a molecule is the mass, in grams, equal to the molecular weight of the substance (the sum of the atomic weights (at. wt.) of the

## Box 1.1 Avogadro and his number

Avogadro's constant (or number),  $N_A$ , is arguably the most fundamental constant in chemistry. Although  $N_A$  is named for Amedeo Avogadro (1776–1856), an Italian scientist born in Turin, he actually did not measure its value or even define it precisely. Instead, Avogadro hypothesized in 1811 that equal volumes of all gases at the same temperature and pressure contain the same number of molecules. The Austrian physicist Johann Loschmidt is credited as the first person to evaluate the constant. Using the kinetic theory of gases, he computed the number of particles per unit volume of an ideal gas (the number of particles per cubic centimeter of gas at standard conditions), which is proportional to but not the same as  $N_A$ . The French Nobel Prize winner Jean Perrin was the first to propose naming the constant in honor of Avogadro, but it was not until the 1930s that use of the term became common. The precise value of  $N_{\Delta}$  was uncertain until fairly recently. Values reported in the late nineteenth and early twentieth centuries ranged from Kelvin's estimate of  $5 \times 10^{23}$  to Perrin's estimate of  $6.5-6.9 \times 10^{23}$ . The currently accepted value is  $6.02214179 \pm 0.00000030 \times 10^{23}$ . In 1960, Avogadro's number was defined as the number of atoms in exactly 12 g of the <sup>12</sup>C isotope of carbon, and a mole was defined as one Avogadro number of atoms or molecules (or any other entity). The International System of Units (SI) adopted the mole as a fundamental unit in 1971 and reversed the above definitions: a mole was defined as the number of atoms in 12 g of <sup>12</sup>C, with a dimension of "amount of substance," and Avogadro's number became a physical constant with units of reciprocal moles ( $mol^{-1}$ ).

atoms in the formula of the molecule). This quantity, the molecular or formula weight in grams, is called the gram-molecular weight or gram-formula weight of a compound. As indicated above, it contains  $6.022 \times 10^{23}$  molecules (or formulas) of the compound. The term "mole," however, is used to express this number of anything atomic particles, grains of sand, stars in the sky. A mole of electrons is  $6.022 \times 10^{23}$ electrons, and this is known as a coulomb. A mole of photons is called an einstein. A gram-atomic weight of an element (its atomic weight in grams) contains 6.022 ×  $10^{23}$  atoms and is a mole of the element.

It is also useful to recall here that the atomic weight of any element approximately is equal to the sum of the number of protons plus the number of neutrons in the nucleus of atoms of the element. The number of protons defines the element's identity and is called the atomic number (at. no.). Fractional atomic weights for some elements result from the contributions of several isotopes (i.e., atoms having the same number of protons but different numbers of neutrons). For example, chlorine (at. no. 17) is a mixture primarily of two stable (i.e., not radioactive) isotopes: ~76% <sup>35</sup>Cl and ~24% <sup>37</sup>Cl; hence, its atomic weight is 35.45.

The standard mass/mass concentration unit in chemistry is *molality* (m):

molality (m) = 
$$\frac{g \text{ of solute}}{g \text{ formula } wt. \times kg \text{ of solvent}}$$
. (1.2)

This unit is used rarely in freshwater chemistry, but it is the unit of choice for precise measurements in marine chemistry and chemical thermodynamics. For dilute solutions, molarity and molality essentially are equivalent, but in solutions as concentrated as seawater (and higher), the equivalency breaks down (see Example 1.2). Molality is temperature invariant, but molarity is not.

### Example 1.2 Molarity and molality of chloride in seawater

The salt content, or salinity (S), of "mean standard" seawater is 35.00% (i.e., 35.00 g/kg seawater). The chlorinity (chloride content) of seawater is related to salinity by the formula:  $S\% = 1.80655 \times Cl\%$ . What is the molality and molarity of chloride in average seawater at 25 °C?

Answer: For the mass basis, we find the [Cl-] by substitution into the relation

$$[Cl^{-}] = (35.00/1.80655 = 19.374\%)$$
, or  $19.374 \text{ g Cl}^{-}/\text{kg}$  seawater,

The density of seawater at 25 °C is 1023.343 kg/m $^3$  or 1.023343 kg/L. $^{16}$  The volume occupied by 1 kg of seawater thus is

$$1.000 \text{ kg} \div 1.02334 \text{ kg/L} = 0.97719 \text{ L (or } 977.19 \text{ mL)}.$$

For the volume basis,  $[Cl^-] = 19.374 \text{ g}/0.97719 \text{ L} = 19.826 \text{ g/L}$ , and the molar concentration is

$$[Cl^{-}] = \frac{19.826 \text{ g/L}}{35.45 \text{ g/mol}} = 0.5593 \text{ mol/L or } \mathbf{0.5593 M}.$$

Because molality is moles of solute per kilogram of water, we need to find how many moles of  $H_2O$  are in 1 kg of seawater. From above, it is clear that 1 kg of seawater contains 35 g of salt. Thus, 1 kg of seawater contains 1,000 – 35 = 965 g  $H_2O$ . Because we calculated that 1 kg of seawater contains 19.374 g  $Cl^-$ , the molality of  $Cl^-$  thus is

$$[Cl^{-}] = \frac{19.374 \text{ g}}{0.965 \text{ kg H}_2O \times 35.45 \text{ g/mol}} = 0.5663 \text{ mol/kg H}_2O \text{ or } \mathbf{0.5663 m}.$$

The difference between the molar and molal concentrations thus is 0.007, or about 1.2%.

It is simple to convert between common and chemical units of concentration: one multiplies chemical units (M, mol/L) by the gram formula weight of the substance (g/mol) to obtain common units (g/L) and divides common units by the formula weight to get chemical units (see Example 1.3). For example, sulfate ion ( $SO_4^{-2}$ ) has a formula weight of 96 g/mol (or 96 mg/mmol) (S = 32; O = 16). A water containing 24 mg/L of sulfate thus has 24 mg/L divided by 96 mg/mmol = 0.25 mmol/L of sulfate. Usually, we say the sulfate concentration is 0.25 millimolar (mM).

Another mass/mass unit of concentration is the *mole fraction*. For any substance X, the mole fraction of X in a system is simply the moles of X divided by the total moles of all substances in the system:

mole fraction of 
$$i = \frac{\text{moles of } i}{\sum_{i=1}^{n} \text{moles of } i}$$
. (1.3)

For example, for a 1.0 M solution of NaCl in water, the mole fraction of NaCl is  $\sim 1/(1+55.5)$ , where 55.5 is the number of moles of water in a liter (1 L × 1,000 g/L × mol/18 g = 55.5 mol). Mole fraction units are not commonly used in inorganic solution chemistry but often are used in the solubility of organic substances in water and in thermodynamic treatment of solid phases associated with natural aquatic systems.

An additional mass/volume chemical unit of considerable importance is *normality* (N). This unit is similar to molarity except that the amount of the substance is based on its reactive capacity with regard to some type of chemical reaction. For acid-base reactions, the basis is the quantity of substance that can accept or donate one mole of hydrogen ions. For oxidation-reduction reactions, it is the amount that can accept or release one mole of electrons. This quantity of a substance is called an *equivalent*, and a solution containing one equivalent (of any substance) per liter has a concentration of one normal (1 N):

Normality (N) = 
$$\frac{grams \ of \ solute}{g \ eq. \ wt. \ of \ solute \times volume \ of \ solution \ (L)}.$$
 (1.4)

The *equivalent weight* of a substance is equal to the molecular (or formula) weight divided by its reactive capacity,  $r_c$ :

Equivalent weight (g) = 
$$\frac{Molecular (formula) weight (g)}{reactive capacity, r_c},$$
 (1.5)

where  $r_c$  is the number of  $H^+$  ions a substance can gain or lose in acid-base reactions or the number of electrons a substance can gain or lose in redox reactions. For electroneutrality (charge-balance) calculations,  $r_c$  is the absolute value of the charge on the ion. Because these quantities may differ for a given substance, equivalent weight is a potentially ambiguous term and the basis for calculation must be specified.

Normality is used in chemistry to express concentrations of titrants. For example, the concentration of an acid used to titrate a basic solution is expressed in terms of normality (N or eq/L). One special case often used in water chemistry, alkalinity, defined as the sum of the "titratable bases in water," may be expressed in milliequivalents per liter (meq/L) or microequivalents per liter (µeq/L), if levels are low.

## Example 1.3 Interconversion among common and chemical concentration units

The major ion concentrations of "global-average" river water  $^{17}$  are reported in mg/L in the first row of numbers below, and the atomic or formula weights of the ions (in grams per mole (g/mol) or milligrams per millimole (mg/mmol)) are given in the next row. Convert the mass concentrations to molar and (charge) equivalent concentrations.

Ion	Na <sup>+</sup>	$K^{\scriptscriptstyle +}$	$Mg^{2+}$	$Ca^{2+}$	$HCO_3^-$	$SO_4^{2-}$	Cl-
Concentration (mg/L)	9.0	1.4	5.0	21	68	20	8
Atomic or formula weight	22.99	39.10	24.30	40.08	61.02	96.07	35.45

Answer: To convert from mg/L to mol/L, we divide the concentrations in mg/L by the atomic or formula weights (g/mol or mg/mmol) to get mmol/L. For example, for Mg<sup>2+</sup>,

1.  $5.0 \text{ mg/L} \div 24.3 \text{ mg/mmol} = 0.206 \text{ mmol/L or } 0.206 \text{ mM}.$ 

Results for all the major ions are shown in the first row of numbers below. Similarly, to convert the concentrations to a charge equivalent basis (meq/L), we divide the mass concentration by the equivalent weight, which for each ion is its atomic (or formula) weight divided by the absolute value of the charge on each ion. Again, for Mg<sup>2+</sup>, we have

2. 
$$5.0 \text{ mg/L} \div \frac{24.3 \text{ mg/mmole}}{2 \text{ meq/mmole}} = 5.0 \text{ mg/L} \div 12.15 \text{ mg/meq} = 0.412 \text{ meq/L}.$$

Results for all ions are given in the second row of numbers below.

Ion	Na <sup>+</sup>	$K^{+}$	$Mg^{2+}$	$Ca^{2+}$	$HCO_3^-$	$SO_4^{2-}$	Cl <sup>-</sup>
mmol/L	0.391	0.0358	0.206	0.524	1.114	0.208	0.226
meq/L	0.391	0.0358	0.412	1.048	1.114	0.416	0.226

According to the *electroneutrality constraint*, all waters are electrically neutral. That is, the sum of the concentrations of the cations must be equal to the sum of the anion concentrations when both are expressed on a charge equivalents basis. Application of this concept to the results in Example 1.3 yields the following:

Sum of cation concentrations:

$$\sum$$
 Cations = 0.391 + 0.0358 + 0.412 + 1.048 = 1.877 meq/L

Sum of anion concentrations:

$$\sum$$
 Anions = 1.114 + 0.416 + 0.226 = 1.756 meq/L

The cation equivalents thus exceed the anion equivalents by 1.877-1.756=0.121 meq/L, or ~6% of the total equivalent concentration of cations. This magnitude of difference usually is considered acceptable in routine water analyses and probably can be accounted for by analytical errors in the measured values of the cations and anions. Other possible explanations are that (1) the analysis did not include all the major inorganic ions, or (2) unmeasured charged moieties, such as carboxylate groups on natural organic matter, account for the anion deficit. The former explanation is unlikely; in most, but not all cases, the seven ions listed in the table account for the vast majority of the inorganic ions in natural waters.

## Example 1.4 Calculations using chemical concentration units

A. Preparation of acid reagents

1. Concentrated sulfuric acid has a density of 1.83 g/mL. If the concentrated acid is 97% H<sub>2</sub>SO<sub>4</sub>, what is its molarity and normality?

*Answer*: The formula weight of  $H_2SO_4$  is 98 (2 + 32 + 4 × 16). One liter of acid contains

$$0.97 \times 1830 \text{ g/L} = 1775 \text{ g/L}$$

and

$$\frac{1775 \text{ g/L}}{98 \text{ g/mol}} = 18.1 \text{ mol/L or } \sim 18 \text{ M}.$$

Because each mole of  $H_2SO_4$  can release two moles of  $H^+$ , the normality of the acid is twice its molarity. Thus concentrated  $H_2SO_4$  is 36 N.

2. If 2.0 mL of concentrated H<sub>2</sub>SO<sub>4</sub> is diluted with distilled water to 250 mL in a volumetric flask, what is the resulting concentration in units of molarity and normality?

Answer: The 2.0 mL of concentrated H<sub>2</sub>SO<sub>4</sub> contains

 $2 \text{ mL} \times 0.97 \times 1.83 \text{ g/mL} \div 98 \text{ g/mol} = 0.0362 \text{ moles}.$ 

The solution thus is  $0.0362 \text{ moles}/250 \text{ mL} \times 1,000 \text{ mL/L} = 0.145 \text{ M}$  and 0.290 N.

3. What is the volume of the solution in question 2 that should be diluted with distilled water to make a 0.025 N solution of sulfuric acid?

*Answer*: For this problem we can use the *fundamental dilution formula*:

 $V_1N_1 = V_2N_2$ , where  $V_1$  and  $N_1$  are the volume and normality of the initial (or "stock") solution and V<sub>2</sub> and N<sub>2</sub> are the volume and normality of the diluted solution. Thus,

$$(0.29 \text{ N})V_1 = (0.025 \text{ N})(1000 \text{ mL}),$$

or

$$V_1 = 86.2 \text{ mL}.$$

Note: Reagent grade concentrated sulfuric acid is not pure acid and contains 96–98% H<sub>2</sub>SO<sub>4</sub>. A solution containing an exact concentration of acid thus cannot be prepared by simple dilution. It is necessary to determine the exact normality by titrating (i.e., reacting) the acid with a basic solution whose normality is known exactly. This process is called standardization. Because of this, one would not bother to measure the stock solution (V<sub>1</sub>) to three-place accuracy; instead, one would measure out ~85 mL by pipette (or graduated cylinder) and separately determine the exact normality of the diluted acid by titration (see Chapter 7).

#### B. Preparation of standard solutions of oxidizing agents

Potassium dichromate is a strong oxidizing agent used in the analysis of "chemical oxygen demand" (COD), a method used, primarily in the past, to estimate the total organic matter in wastewater samples.<sup>18</sup> In the process of oxidizing the organic matter, dichromate ion, Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, is reduced to two chromic ions, Cr<sup>3+</sup>, which involves transfer of six electrons to dichromate:

4. Exactly how many grams of reagent-grade K<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub> must be weighed out and added to water to prepare a 1.0 L of a solution that is exactly 0.25 N  $K_2Cr_2O_7$ , and what is its molarity?

Answer: The formula weight of  $K_2Cr_2O_7$  is  $(2\times39.1)+(2\times52)+(7\times16)=294.2$ . Its equivalent weight thus is  $294.2\div6=49.033$  g. To make a 1.0 L solution containing 0.250 eq/L of dichromate, we need to weigh out 0.250 eq  $\times$  49.033 g/eq = 12.258 g. The molarity of the solution is 0.25 eq/L  $\div$  6 eq/mol = 0.04167 mol/L.

# 1.3.4 Other concentration units used in environmental chemistry

The units described in the previous sections are the preferred ways to express concentrations of chemicals in water and generally are the most commonly encountered units today. A few other units, however, are used in environmental engineering and water chemistry. We describe and define these units below.

mg/L as calcium carbonate ( $CaCO_3$ ). This unit was used in natural water chemistry to express concentrations of alkalinity, hardness, and ions related to these terms. Although now used only rarely in scientific literature, it still is in wide use within the water treatment industry. *Alkalinity* is defined as the sum of the concentration of bases titratable with strong acid and is closely related to the bicarbonate concentration in natural waters (see Chapter 8). *Hardness* is the sum of the divalent cations (generally  $Ca^{2+}$  and  $Mg^{2+}$ , but occasionally  $Fe^{2+}$  and  $Mn^{2+}$ ), which cause problems with soap precipitation and buildup of  $CaCO_3$  scale in pipes (see Chapter 10).

The unit mg/L as  $CaCO_3$  is based on the fact that  $CaCO_3$  has a formula weight of  $100 \ (40 + 12 + (3 \times 16))$  and an equivalent weight of 50, in terms of its reacting capacity with H<sup>+</sup> and the charge equivalents of its constituent ions. Thus,  $50 \ g$  of  $CaCO_3$  yields  $0.5 \ moles$  of carbonate and requires  $1.0 \ moles$  of H<sup>+</sup> to be titrated to  $CO_2$  (see Chapter 8);  $50 \ g$  of  $CaCO_3$  also yields one equivalent (or one mole) of cationic and anionic charges. The unit expresses concentrations of  $Ca^{2+}$ ,  $Mg^{2+}$ , hardness, or alkalinity as if the constituents all have an equivalent weight of 50. As a "pseudo-equivalents per liter" or "pseudo-normal" unit, it is convenient in that concentrations expressed this way can be added in a meaningful way. For example,  $[Ca^{2+}] + [Mg^{2+}]$  (each expressed in mg/L as  $CaCO_3$ )  $\approx$  total hardness (in mg/L as  $CaCO_3$ ). In contrast,  $[Ca^{2+}] + [Mg^{2+}]$  (each expressed in mg/L) is not chemically meaningful.

To convert from the preferred chemical units of alkalinity (meq/L) to mg/L as CaCO<sub>3</sub>, we multiply the former by the equivalent weight of CaCO<sub>3</sub>:

Alkalinity (mg/L as 
$$CaCO_3$$
) = Alkalinity (meq/L)  
× (50 mg  $CaCO_3$  / meq of  $CaCO_3$ ) (1.5)

Alkalinity (mg/L as 
$$CaCO_3$$
) = Alkalinity ( $\mu eq/L$ )  
  $\times (0.050 \text{ mg/}\mu eq \text{ of } CaCO_3).$  (1.6)

Conversely,

Alkalinity (
$$\mu eq/L$$
) = 20 × Alkalinity (mg / L as CaCO<sub>3</sub>). (1.7)

To convert between units of mg/L for Ca<sup>2+</sup> and Mg<sup>2+</sup> and units of mg/L as CaCO<sub>3</sub>, we divide the former by the equivalent weight of the atom (to obtain the number of equivalents of Ca or Mg) and multiply by the equivalent weight of CaCO<sub>3</sub>:

$$Ca^{2+}$$
 (mg/L as  $CaCO_3$ ) =  $\frac{\text{mg/L as Ca}}{20 \text{ mg/meq of Ca}} \times 50 \text{ mg/meq of CaCO}_3$  (1.8)

$$Mg^{2+}$$
 (mg/L as CaCO<sub>3</sub>) =  $\frac{mg/L \text{ as Mg}}{12.15 \text{ mg/meq of Mg}} \times 50 \text{ mg/meq of CaCO}_3$  (1.9)

## Example 1.5 Conversion of alkalinity and hardness units

1. The sensitivity of surface waters toward acidification from atmospheric acid deposition is inversely related to the water body's alkalinity (also called acid-neutralizing capacity, ANC). Water with an alkalinity less than 200 μeg/L is considered "acid sensitive." What is this alkalinity value in mg/L as CaCO<sub>3</sub>?

#### Answer:

 $200 \mu \text{eg/L} \times 50 \text{ mg CaCO}_3/\text{meg} \times 10^{-3} \text{ meg/\mu eg} = 10 \text{ mg/L as CaCO}_3$ .

2. Lake Okeechobee in south Florida is a large, shallow, hardwater lake with high concentrations of Ca<sup>2+</sup> and Mg<sup>2+</sup>, typical values of which in the lake are  $[Ca^{2+}] = 45 \text{ mg/L}$  and  $[Mg^{2+}] = 18 \text{ mg/L}$ . Convert these values to concentrations in mg/L as CaCO<sub>3</sub> and evaluate the total hardness of the lake.

#### Answer:

```
[Ca^{2+}] = 45 \text{ mg/L} \div 40 \text{ mg/mmol} = 1.125 \text{ mmol/L of } Ca^{2+}
1.125 \text{ mmol/L} \times 2 \text{ meg/mmol} = 2.25 \text{ meg/L of Ca}^{2+}
[Ca^{2+}] = 2.25 \text{ meg/L} \times 50 \text{ mg/meg CaCO}_3 = 112.5 \text{ mg/L as CaCO}_3.
[Mg^{2+}] = 18 \text{ mg/L} \div 24.3 \text{ mg/mmol} = 0.74 \text{ mmol/L of } Mg^{2+}
0.74 \text{ mmol/L} \times 2 \text{ meq/mmol} = 1.48 \text{ meq/L of Mg}^{2+}
```

$$\begin{split} [Mg^{2+}] &= 1.48 \text{ meq/L} \times 50 \text{ mg/meq CaCO}_3 = 74 \text{ mg/L as CaCO}_3 \\ &\text{Total hardness} = [Ca^{2+}] + [Mg^{2+}] \text{ (both in mg/L as CaCO}_3) = 112.5 + 74 \\ &= 186.5 \text{ mg/L as CaCO}_3 \end{split}$$

mg/L as N or P (or mg N/L; mg P/L). These units are used in water quality and limnological studies and express concentrations of various chemical forms of nitrogen or phosphorus in terms of the amount of elemental N or P present. This convention is useful for several reasons. From an algal nutritional point of view, one is not interested in the concentration of nitrate or ammonium ion, for example, but in the amount of N in the nitrate or ammonium, the actual part of the ion needed by organisms. Also, because these are pseudo-molar units, we can add concentrations of various species if they are expressed in terms of N (or P), but we cannot meaningfully add concentrations of ammonium and nitrate when they are expressed in mg/L of the ions themselves.

To convert from mg/L of an N-containing species to mg/L as N, one divides the former by the formula weight of the species and multiplies the result by 14, the atomic weight of nitrogen. For nitrate,

$$\mathbf{NO}_{3}^{-} \text{ (mg/L as N)} \\
= \frac{\text{mg/L of NO}_{3}^{-}}{62 \text{ mg/mmol}} \times (14 \text{ mg/mg-atom}) \times (1 \text{ atom N/molecule of NO}_{3}^{-}).$$
(1.10)

For ammonium,

$$\mathbf{NH}_{4}^{+}(\text{mg/Las N}) = \frac{\text{mg/Lof NH}_{4}^{+}}{18 \,\text{mg/mmol}} \times (14 \,\text{mg/mg-atom}) \times (1 \,\text{atom N/molecule of NH}_{4}^{+}). \tag{1.11}$$

Similarly, for phosphate,\*

$$PO_4^{3-} (mg/L \text{ as P})$$

$$= \frac{mg/L \text{ of PO}_4^{3-}}{95 \text{ mg/mmol}} \times (31 \text{ mg/mg-atom}) \times (1 \text{ atom P/molecule of PO}_4^{3-}).$$
 (1.12)

<sup>\*</sup> The actual form (degree of protonation) of inorganic phosphate in water depends on pH.  $PO_4^{3-}$  is important only at very high pH values. Consequently, phosphate usually is reported as "dissolved inorganic P" or "dissolved reactive P" (DRP), reflecting the operational nature of the analytical results (see Chapter 19).